

# GIS-BASED ELABORATE SPATIAL PREDICTION OF SOIL NUTRIENT ELEMENTS USING ANCILLARY TERRAIN DATA IN CHONGQING TOBACCO PLANTING REGION, CHINA

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**Abstract:** The precision agriculture hopes to manage the variation in soil nutrient status continuously, which requires reliable predictions at places between sampling sites. For the long time, ordinary kriging has been used as one prediction method when the data are spatially dependent and a suitable variogram model exists. However, even if data are spatially correlated, there are often few soil sampling sites in relation to the area to be managed. Recently, Digital elevation models (DEMs) and remotely sensed data are becoming more readily available, these data are usually far more intensive than those from soil surveys. If these ancillary data are coregionalized with the sparse soil data, they might be used to increase the accuracy of predictions of the soil properties.

Under ArcGIS platform, this paper employed spatial predictions of the soil total N, P, K in Chongqing tobacco planting region, China, with cokriging and regression kriging respectively. For the both, intensive terrain data including elevation, slope and aspect were used with the soil data. Traditional ordinary kriging (OK) was investigated as comparison basis to determine which approach is appropriate for different soils properties mapping. And the results suggest that the use of intensive ancillary data can increase the accuracy of predictions of soil properties in arable fields provided that the variables are related spatially.

Keywords: Ordinary kriging, Cokriging, Regression kriging, Ancillary terrain data, Soil nutrient elements, Elaborate spatial prediction

## 1. INTRODUCTION

One aim of regional precision agriculture is to use information about spatial distribution of soil properties to manage the field in a landscape-specific way, for example, by the application of nutrients at the places and in the amounts required (Sylvester-Bradley et al., 1999). Sampling at discrete places is the traditional means of obtaining information about the soil properties. However, field surveys are often time-consuming, labor-intensive and costly although it is still the dominant way to obtain information about most soil properties. Predicting unsampled sites by available sampling points data with acceptable precision and cost hence has been the focus of pedometrics (Webster, 1985; Cambardella et al., 1994; Goovaerts, 1997; McBratney et al., 2000; Auemhammer, 2001). Traditionally, this has been achieved by classification, but it has been known for some time that this approach does not describe adequately the variation that scientists and farmers are aware of intuitively (Webster and Oliver, 2001). Ordinary kriging (OK) is quite suited to this problem provided that the data are spatially dependent (Webster and Oliver, 2001). However, the data from soil surveys, are often sparse even though they might be spatially autocorrelated and it can lead to considerable uncertainty in the kriging prediction (McBratney et al., 2000). Also, the precision of the prediction was shown to be very sensitive to the density of observation points and the gains in precision were only slight for sites located near from the observation sites (Auemhammer, 2001).

A way of refining these predictions could be to use easy-to-measure auxiliary data describing landscape features. Particularly, the use of attributes derived from Digital Elevation Models (DEMs) which becomes more readily available looks promising since some researchers have demonstrated the relationships between landforms features and soil properties (Chaplot et al., 2004; Lopez-Granados et al., 2005; Kay and Rainer, 2008; Wu et al., 2008). Recently several predictive soil attributes techniques that use intensive auxiliary data also have been developed, for example, cokriging and regression kriging.

Chongqing tobacco planting region, which locates in one of the poorest areas of southwest China and mostly is covered by hilly and mountains. Understanding how soil nutrients vary across landscape positions especially increasing the accuracy of spatial prediction of soil nutrient elements would be of huge economic and environmental benefit for local tobacco planting

and management. This study predicted spatial distribution of total N, P, K of this region by cokriging and regression kriging respectively in which intensive terrain properties including elevation, slope and aspect were used as auxiliary data. Traditional ordinary kriging interpolation was investigated as comparison basis to determine which approach is the appropriate method for different soil nutrient elements spatial distribution.

This paper is organized as follows. Following the introduction, theory and methods used in this study are described in section 2. The study area and data are depicted in section 3. In section 4, results and discussion are illustrated. Conclusion is finally made in section 5.

## 2. THEORY AND METHODS

Ordinary kriging, cokriging and regression kriging were used in this study. The last two are described briefly below (for ordinary kriging, see (Webster and Oliver, 2001) )

### 2.1 Cokriging

Cokriging is an extension of ordinary kriging that takes into account the spatial cross-correlation from two or more variables. The usual situation is one where the primary or target variable,  $Z_u(x)$ , has been measured at many fewer places,  $x$ , than the secondary one,  $Z_v(x)$ , with which it is coregionalized. We assume that they obey the intrinsic hypothesis. Both variables have an autovariograms, for variable  $u$ , this is

$$\gamma_{uu}(h) = \frac{1}{2} \left[ \{z_u(x) - z_u(x+h)\}^2 \right] \quad (1)$$

Where  $h$  is a vector, the lag. For  $v$  also, the expected differences are zero and its autovariogram is  $\gamma_{vv}(h)$ . The two variables have a cross-variogram,  $\gamma_{uv}(h)$ , defined as

$$\gamma_{uv}(h) = \frac{1}{2} E[\{Z_u(x) - Z_u(x+h)\}\{z_v(x) - z_v(x+h)\}] \quad (2)$$

Which describes the way in which  $u$  is spatially related to  $v$ .

To compute the usual cross-variogram, there must be sites where both  $u$  and  $v$  have been measured, i.e., collocated. The experimental cross-variogram,  $\hat{r}_{uv}(h)$  can be estimated by

$$\hat{\gamma}_{uv}(h) = \frac{1}{2m(h)} \sum_{i=1}^{m(h)} \{z_u(x_i) - z_u(x_i + h)\} \{z_v(x_i) - z_v(x_i + h)\} \quad (3)$$

Where  $z_u$  and  $z_v$  have been measured at sites  $x_i$  and  $x_i + h$ , and  $m(h)$  is the number of pairs of data points separated by the particular lag vector  $h$ .

The cross-variogram can be modeled in the same way as the auto-variogram, but there is an added condition. Any linear combination of the variables it itself a regionalized variable, and its variance must be positive or zero. This is ensured if we adopt the linear model of coregionalization. For any pair of variables  $u$  and  $v$ , the variogram is

$$\gamma_{uv}(h) = \sum_{k=1}^k b_{uv}^k g_k(h) \quad (4)$$

Where the  $b_{uv}^k$  are the variances, for example the nugget and sill variances.  $g_k(h)$  is the spatial autocorrelation function which must be the same for both variables being analyzed.

The ordinary punctual cokriging prediction of the primary variable,  $Z_u$  is obtained from the linear sum

$$\hat{Z}_u(x_0) = \sum_{i=1}^V \sum_{l=1}^{n_l} \lambda_{il} z_l^{ok}(x_i) \quad (5)$$

Where there are  $V$  variables,  $l=1,2,\dots,V$ , of which  $u$  is the one to be predicted, and the subscript  $i$  refers to the sites of which there are  $n_l$  in the search neighborhood where the variable  $l$  has been measured. The  $\lambda_{il}$  are the weights, which in the case of 'classical' cokriging (Goovaerts, 1997) satisfy

$$\sum_{i=1}^{n_l} \lambda_{il} = \begin{cases} 1, & l = u \\ 0, & l \neq u \end{cases} \quad (6)$$

There are the non-bias conditions, and subject to them the weights,  $\lambda_{il}$ , that minimize the estimation variance of  $\hat{Z}_u$  for a point,  $x_0$ , are found by solving the kriging system for all  $v=1,2,\dots,V$  and all  $j=1,2,\dots,n_v$ . The weights  $\lambda_i$  are inserted into Eq.(5) to estimate  $Z_u(\hat{x}_0)$ .

## 2.2 Regression kriging

Odeh et al.(Odeh et al., 1995) describe three types of regression kriging: model A, B and C which are developments of the general theme. For this study, we used model C, which we summarize here. The method is based on a linear regression between a target variable such as certain soil property ( $Z$ ), and a secondary or third variable, such as elevation or slope ( $Y_i$ ). The regression model so obtained is used to predict  $Z$  to the locations of the

prediction grid at which  $Y_i$  is known. The residuals from the regression  $\varepsilon$  are kriged to the prediction grid using the variogram computed from the residuals. The predicted values  $\hat{z}_R$  and the kriged values of the residuals  $\hat{\varepsilon}_{ok}$  are summed to give the predicted values of the target variable  $\hat{z}_{RK}$ .

$$\hat{z}_{RK}(x) = \hat{z}_R(x) + \hat{\varepsilon}_{ok}(x) \quad (7)$$

### 2.3 Performance evaluation indicators

In order to evaluate the performance of different spatial prediction methods, mean squared error(MSE) and root mean squared standardized effect(RMSSE), in this paper are used as performance measure indicators.

The mean squared error(MSE) is expressed as

$$MSE = \frac{1}{l} \sum_{j=1}^l [z_1(x_i) - z_2(x_i)] \quad (8)$$

The root mean squared standardized effect(RMSSE) is expressed as

$$RMSSE = \sqrt{\frac{1}{l} \sum_{i=1}^l [z_1(x_i) - z_2(x_i)]^2} \quad (9)$$

Where  $z_1(x_i)$  is standardized site true value and  $z_2(x_i)$  represents standardized site prediction value,  $l$  is the number of validation sites. When MSE is more close to 0 and RMSSE more approaches 1, the accuracy of prediction is hold higher.

## 3. THE STUDY AREA AND DATA SOURCES

### 3.1 The study area

The study area is located in the east part of Chongqing between north latitudes  $28^{\circ} 09'$  and  $32^{\circ} 12'$  and east longitudes  $106^{\circ} 23'$  and  $110^{\circ} 11'$  (Fig.1).The climate is characterized by an average annual temperature between  $10.1$  and  $18.2^{\circ}\text{C}$ . Annual precipitation is about  $1200\text{mm}$ . According to Chinese Soil Taxonomy, the soils are classified by yellow soil, yellow brown soil, limestone soil, purple soil and paddy soil.

The landform of study area is dominated by hills, low mountains and medium mountains. Generally, it is undulating with slopes ranging from 0 to 84 ° and altitudes within the range from 100 to 2750.92 m. Due to weak transportation and economy development, tobacco planting is one of local dominant crops productions.

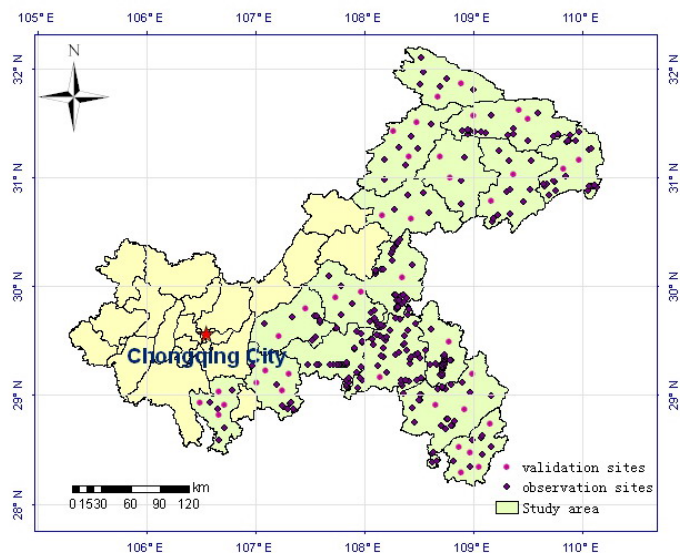


Fig.1: Location of the study area

### 3.2 Data sources

The soil was sampled in the spring of 2007 at 300 sites of 17 tobacco planting counties at a depth of 0-20cm. The position of each site was georeferenced using a DGPS(Differential Global Positioning System). From the observations, 40 sites, randomly selected, were kept aside for validation(the validation set).Therefore, the 260 remainder sites formed the prediction set.

The field soil was analyzed for total Nitrogen(N),Phosphorus(P) and  $K_2O$  as soon after sampling as possible. Kjeldahl method was utilized to measure the soil total N , and the total P and  $K_2O$  were determined by x-ray fluorescence(XRF) analysis(Lu and Yang, 1993) .

A DEM was constructed using ArcMAP Version 9.2(ESRI).  $50 \times 50m$  DEM data were derived from automated image matching of scanned panchromatic aerial photograph based on AUNDEM(Auemhammer, 2001) . Primary terrain attributes including elevation, slope and aspect were extracted by ArcMAP spatial analyst module.

## 4. RESULTS AND DISCUSSION

### 4.1 Exploratory data analysis

Table 1 list the descriptive statistics of total N,P and K<sub>2</sub>O in the study area. The K-S test indicates that the whole dataset all followed a normal distribution.

Table 1. Descriptive statistics for Total N,P, K<sub>2</sub>O

Item	Mean	Min	Max	Skewness	S.D	K-S
Total N(ug/g)	1534.40	798.64	2933.	0.89	356.70	0.21
Total P(ug/g)	717.50	299.10	1448.90	0.78	202.34	0.17
Total K <sub>2</sub> O(%)	2.41	0.68	5.66	0.65	0.74	0.15

The Pearson product moment correlation coefficients were calculated between the total N,P, K<sub>2</sub>O and elevation, slope and aspect from the co-located data to determine whether it was feasible to use these terrain data to improve their prediction. Table 2 gives the correlation coefficients of N,P and K<sub>2</sub>O with terrain data. For all three soil nutrients, they all related to elevation and ranged from weak for K<sub>2</sub>O,to moderate for P and strong for N. For slope, both N and P were inversely related but K<sub>2</sub>O is likely to be indirect. Besides K<sub>2</sub>O, the other soil elements have no obvious links with aspect.

Table 2. Pearson product moment correlation coefficients between soil nutrients and terrain data

Item	Elevation	Slope	Aspect
Total N	0.295*	0.173*	-0.026
Total P	0.179*	0.116*	-0.051
Total K <sub>2</sub> O	0.113*	0.075	-.132*

### 4.2 Cokriging

Experimental cross- and auto-variograms were obtained by applying Eq.(4) using the DEM predictions of elevation, slope and aspect at the observation sites. We fitted the models of coregionalization to soil total N,P, K<sub>2</sub>O and three terrain attributes. It is shown as in table 3.

It was indicated that the two sets variograms of elevation, slope for N and P were both bounded and were fitted by exponential, spherical ,Gaussian, spherical function respectively. The variograms of aspect for N and P were unbounded, whereas it it was bounded for K<sub>2</sub>O with the range set to

121.04.Under the ArcGIS platform, elevation, slope were associated as covariances for N,P spatial prediction and elevation, aspect covariances for K<sub>2</sub>O spatial prediction. The whole prediction maps were shown in Fig.2.

Table3 Variogram model parameters with elevation, slope and aspect of soil nutrients

Item	Variable	Model	Nugget	Sill	Range(Km)
N	Elevation	Exponential	0.69	0.90	141.163
	Slope	Spherical	1.13	1.21	320.606
	Aspect	Linear	1.21		
P	Elevation	Gaussian	0.71	0.88	118.198
	Slope	Spherical	1.13	1.21	320.606
	Aspect	Linear	1.21		
K <sub>2</sub> O	Elevation	Exponential	0.61	0.89	117.379
	Slope	Linear	0.71		
	Aspect	Spherical	0.62	1.01	121.04

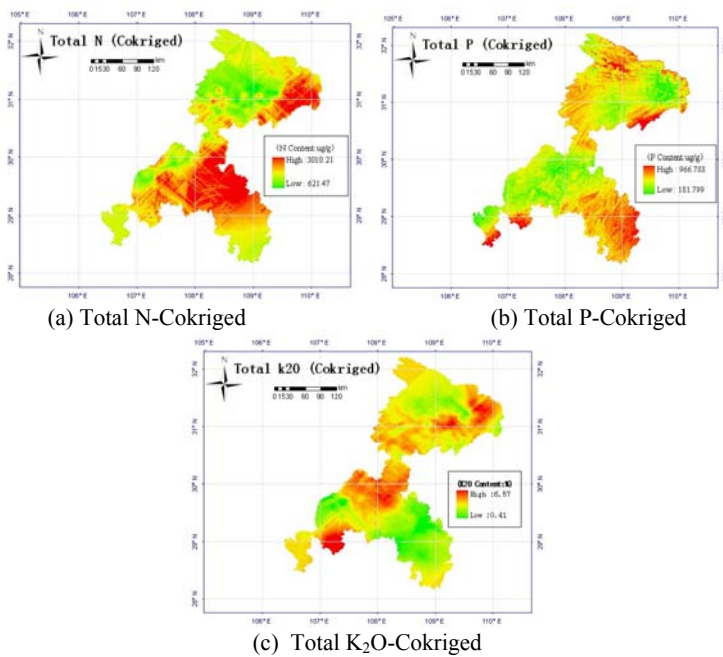


Fig.2 Spatial distribution for total N, P, K<sub>2</sub>O with cokriging

### 4.3 Regression kriging

Linear regressions of total N,P, K<sub>2</sub>O were done on the DEM data at the observation sites. The equations were depicted as follows:

$$Y_1 = 0.482h + 1.8\alpha - 0.151\beta + 128.067 \quad (r^2=0.635) \tag{10}$$

$$Y_2 = 0.32h + 0.751\alpha + 0.205\beta - 263.189 \quad (r^2=0.517) \tag{11}$$



$$Y_3 = 0.001h + 0.003\alpha - 0.001\beta + 2.254 (r^2=0.611) \quad (12)$$

where  $Y_1, Y_2$  and  $Y_3$  represents total N, P,  $K_2O$  respectively,  $h, \alpha, \beta$  represents elevation, slope and aspect.

An experimental variogram was also computed on the residuals of total N, P and  $K_2O$  from the regression at each site. It is shown as table 4.

Table 4 Parameters for the fittest residuals theoretical models of total N,P, $K_2O$

Item	Model	Nugget	Sill	Range(km)	C/C <sub>0</sub> +C	R <sup>2</sup>
N residuals	Spherical	7.94	10.99	211.40	0.72	0.872
	Exponential	6.05	10.61	114.601	0.57	0.958
	Gaussian	7.11	10.41	75.820	0.68	0.811
P residuals	Spherical	11.77	29.49	81.259	0.40	0.672
	Exponential	4.94	29.68	78.022	0.17	0.713
	Gaussian	15.23	29.53	72.210	0.52	0.966
$K_2O$ residuals	Spherical	0.15	0.23	72.651	0.65	0.753
	Exponential	0.12	0.24	57.718	0.50	0.821
	Gaussian	0.16	0.23	54.479	0.70	0.934

It was found that the highest determined coefficient(R<sup>2</sup>) existed in Exponential, Gaussian, Gaussian Model for total N,P,  $K_2O$  residuals respectively. The whole spatial prediction map is displayed in Fig.3.

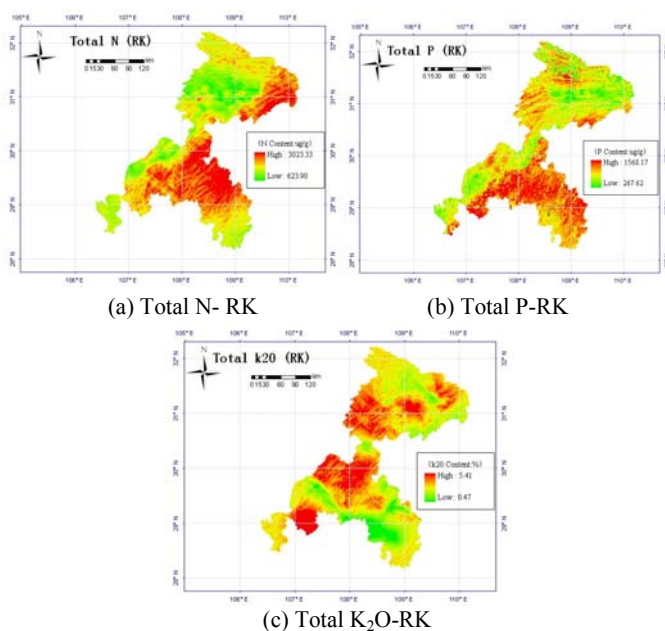


Fig.3 Spatial distribution for total N, P, $K_2O$  with regression kriging

### 4.4 Ordinary kriging

Different semivariogram models for models for the soil N,P,K<sub>2</sub>O were presented in Table 5.

Table 5 Parameters for the fittest residuals theoretical models of total N,P,K<sub>2</sub>O

Item	Model	Nugget	Sill	Range(km)	C/C <sub>0</sub> +C	R <sup>2</sup>
N	Spherical	0.94	1.29	11.811	0.73	0.731
	Exponential	0.77	1.31	10.235	0.59	0.742
	Gaussian	1.02	3.85	10.496	0.26	0.867
sP	Spherical	2.39	4.50	10.983	0.53	0.821
	Exponential	1.89	4.53	11.378	0.42	0.910
K <sub>2</sub> O	Gaussian	2.74	4.51	9.437	0.61	0.877
	Spherical	4.91	5.68	121.766	0.86	0.726
	Exponential	4.11	5.63	63.034	0.73	0.891
	Gaussian	4.73	5.62	58.767	0.84	0.677

It was found that the highest determined coefficient(R<sup>2</sup>) existed in Gaussian, Exponential, Exponential Model for total N,P, K<sub>2</sub>O respectively. The whole spatial prediction map is displayed in Fig.4.

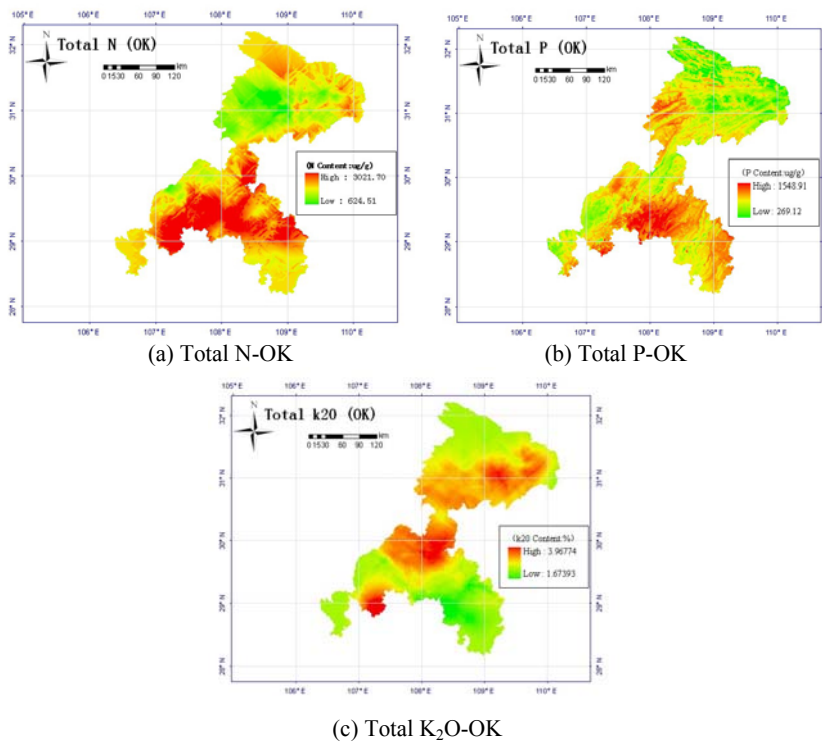


Fig.4 Spatial distribution for total N, ,K<sub>2</sub>O with ordinary kriging

#### 4.5 Discussion

The MSEs and RMMSEs for total N,P, K<sub>2</sub>O are given in table 6 for each method of spatial prediction.

Table 6 MSE and RMSSE between the measured and predicted values at the validation sites

Item		CoK	RK	OK
N	MSE	0.065	0.047	0.091
	RMSSE	0.872	0.911	0.811
P	MSE	0.071	0.082	0.102
	RMME	0.946	0.901	0.777
K <sub>2</sub> O	MSE	0.034	0.027	0.061
	RMSE	0.911	0.973	0.897

For total N, the MSE for regressing kriging was the smallest, followed by that for cokriging, and last was the ordinary kriging. The RMSSE of being close to 1 is ranked by RK,CoK and OK. These results show that that some benefit aroused from using the more intensive terrain data to predict the sparser soil properties.Fig.2,3,4 shows the spatial prediction maps with different methods. Generally, the major patterns of variation are evident but the detail is different. The most variable map is the one from the OK prediction, and the smoothest is from regression kriging.

Table 6 shows that CoK was the most accurate method of prediction for total P, followed by regression kriging, and the ordinary kriging was the worst in this case. The less accurate predictions from regression kriging probably reflect regression model less good determined coefficient .

For total K<sub>2</sub>O ,the prediction accuracy rank shows similar pattern with total N.

### 5. CONCLUSION

Understanding the spatial variation of soil properties to manage the field is one aim of precision agriculture. Increasing the accuracy of the spatial predictions of soil nutrient elements with the aid of available ancillary data is quiet economic and environmental typically in complex terrain hilly areas ,because soil nutrient elements are measured sparsely compared with ancillary data such as elevation, slope and aspect. This study predicted the three soil nutrient elements spatial distribution with CoK, RK and OK in Chongqing tobacco planting area, and the methods of incorporating ancillary terrain data both show good advantage.

With the intensive environmental data like DEM and remotely sensed data from satellites and ground-based systems become increasingly available, they are likely to confer benefit in the context of general environmental management where sampling to record the variable and limits the accuracy of predictions. However, up to now there is no single best method for all variables. The coregionalization and the relations between the deterministic components of the variation should still be examined carefully before deciding on the most appropriate method of prediction.

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