Flow-level Modeling of Multi-User Beamforming in Mobile Networks

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Abstract—Among the several features that are foreseen for increasing the capacity of cellular systems, Multi-user multi-input multi-output (MU-MIMO) is considered as a key enabling technology. Particularly, MU-beamforming is a powerful means of increasing the system capacity and throughput by creating several spatial signals to different users on the same time/frequency resource. In this paper, we develop an analytical model for MU-beamforming based on queuing theory combined with network simulations. The proposed framework is used for evaluating the potential gains in terms of capacity and throughput in LTE-Advanced system. Several scenarios are studied, with and without beamforming, Results show an important gain of SU-beamforming over the classical system without beamforming and a further gain of MU-beamforming, especially at high loads.

Index Terms- Multi-user beamforming, LTE-Advanced, Flow Level Modeling, Queuing Theory, Simulations.

I. INTRODUCTION

Nowadays, the wireless networks industry is moving toward LTE system which is expected to improve the performance in terms of spectral efficiency and user throughput. In its release 8, it enables to achieve 300 Mb/s for the downlink and 75 Mb/s for the uplink with the utilization of OFDM and single user-MIMO (SU-MIMO) transmission. Then, in order to meet the requirements of the IMT-Advanced systems, LTE has been further enhanced to LTE-Advanced which is able to achieve a target throughput of 1 Gb/s on the downlink and 500 Mb/s on the uplink with advanced physical layer techniques [1][2] including carrier aggregation [3], enhanced multi-antenna schemes and Coordinated Multi-Point transmission technique (CoMP) [4]. Particularly, multi-user MIMO (MU-MIMO) is considered as a key enabling technology for LTE-Advanced that enables to achieve the expected performance [5].

Indeed, in downlink MU-MIMO system, the Base Station (BS) creates different spatial signals to multiple Mobile Stations (MS) on the same time/frequency resource. Accordingly, the scheduling opportunities for each MS is largely improved compared to a SU-MIMO system where only a single user exploits the spatial gain offered by multi-antenna systems [6]. However, this operation introduces interference between co-scheduled users within the same cell in addition to the interference from adjacent cells. Therefore, advanced precoding/beamforming techniques and a well designed scheduling scheme need to be implemented in order to combat this intra-cell interference and increase the system capacity.

While a large number of papers deals with the physical layer aspects of MU-MIMO by investigating the optimal schemes with low complexity, we propose in this paper a flow level modeling of MU-MIMO in different scenarios. Indeed, existing performance evaluations of MU-MIMO are based on system-level simulations with a static number of users in different cells (e.g. [7][8][9]); they do not capture the dynamics of users’ behavior in the system. Moreover, they do not reflect the actual distribution of users in the cell since those at cell edge stay longer in the cell for finishing their service due to a low data rate [10]. However, in this work, we propose an analytical method based on queuing theory that captures the dynamics of arrivals and departure processes. It is practically interesting and, to the best of our knowledge, has not been proposed yet.

In this paper, we consider a special MIMO scheme which is transmit beamforming that permits to concentrate the energy towards one or more directions. Particularly, we evaluate the expected gains of MU-beamforming in terms of throughput and capacity in different scenarios. We start with SU-beamforming system, then we investigate the MU-scheduling impact under different network configurations. We propose for each scenario a flow-level model and we evaluate its performance using both Markovian analysis and network simulations in different load conditions. Results show an important gain of SU-beamforming over the classical system without beamforming and a further gain of MU-beamforming, especially at high loads.

The remainder of this paper is organized as follows. Section II presents a basic background of MIMO system and MU-MIMO framework. Section III describes the model used in this paper. We present in section IV the flow-level analysis for the SU-beamforming and the MU-beamforming in the presence of three and four serving beams. Section V gives the results using network simulations. Section VI concludes the paper.

II. BACKGROUND

A. MIMO System

One of the key technique of advanced communication systems is the MIMO transmission which enables multiple antennas at both receiver and transmitter, with additional processing, to improve the system performance in terms of...
coverage, capacity and robustness. There are basically three main advantages from MIMO transmission [11]:

- Diversity gain: by using the spatial diversity provided by the multiple antennas in order to improve the system robustness and reliability.
- Spatial multiplexing gain: by transmitting multiple data streams to a single or multiple users on multiple spatial dimensions (i.e. layers) in order to improve the user’s spectral efficiency.
- Array gain: by concentrating the energy in one or more directions via precoding/beamforming functionality, thus increasing the data rates.

Various scenarios are proposed for LTE downlink; they are referred as Transmission Modes (TM) in releases’ specification. The final MIMO scheme depends on the network deployment and the propagation conditions of the different users.

B. MU-MIMO Framework

The MU-MIMO framework has been introduced for LTE-Advanced standard and considered as a key enabler for achieving high spectral efficiency. It enables a BS to co-schedule a set of MSs on the same time/frequency resource. However, this operation introduces additional intra-cell interference. Therefore, advanced precoding and scheduling methods need to be implemented to get full benefit of MU-MIMO transmission.

1) MU Precoding: The key issue with the MU-precoding is to find a compromise between performance gain, Channel State Information (CSI) requirement and design complexity. The Dirty Paper Coding (DPC) [12] enables to achieve an optimal capacity but is impractical in real systems due to its complexity and full CSI requirement. Alternatively, linear precoding methods, such as zero-forcing (ZF) [13], appear to be more robust to erroneous CSI and with a low complexity relatively to other methods.

2) User selection/scheduling: Different factors affect the MU-scheduler performance including the wireless environment since a minimum separation between users is required. This is only possible through narrow antenna beam patterns. Also, the cell load is an important factor; indeed highly loaded cells provide more user grouping possibilities than lightly loaded cells where it is more efficient to schedule a single user. Different schedulers have been proposed in literature for MU-MIMO (e.g. [14] and reference therein).

Since we consider a beamforming scheme, the MU scheduling can be performed using:

- Max-Sum scheduler. The aim is to find the optimal set of users covered by different beams which maximizes a total utility function.
- Max-iterate scheduler. A first user is chosen according to a certain metric, then users from adjacent beams are blocked and the same process is repeated until reaching the maximum number of active beams or that there are no more users to schedule.

III. Model

A. Physical layer aspects

We consider a downlink multi-user environment consisting on a base station (BS) with $N$ transmit antennas communicating with $M$ mobile stations (MS). We focus on the beamforming system represented by the block diagram shown in figure 1 where the data information blocks are mapped into layers, then to the antenna ports by means of the precoding/beamforming functionality. We investigate two possible schemes [15]: the one-layer beamforming where a single layer is assigned to one MS (i.e. SU-beamforming) and dual-layer beamforming where the two layers are assigned to two separate MSs (i.e. MU-beamforming).

Let $X_i$ and $W_j$ denote the transmitted data intended to user $i$ and its transmit beamforming vector. When one-layer beamforming is used, the received signal at $MS_i$ is given by:

$$Y_i = H_i W_i X_i + I_i + N_i,$$

where $H_i$, $I_i$ and $N_i$ denote the channel gain from the BS to the $i$th MS, the inter-cell interference and an Additive White Gaussian Noise (AWGN) vector at $MS_i$, respectively. The corresponding SINR is given by:

$$\text{SINR}_i = \frac{|H_{ki} W_i|^2}{|I_i|^2 + ||N_i||^2}.$$

However, when dual-layer beamforming is deployed, the received signal at $MS_i$ is expressed by:

$$Y_i = H_i W_i X_i + H_i \sum_{l \neq i} W_l X_i + I_i + N_i,$$

In Equation 1, the four terms represent the desired signal, the multi-user interference, the inter-cell interference and the noise, respectively. Hence, the SINR at user $i$ is:

$$\text{SINR}_i = \frac{|H_{ki} W_i|^2}{|H_i \sum_{l \neq i} W_l|^2 + ||I_i||^2 + ||N_i||^2}.$$

Using the Shannon’s formula, we can express the transmission rate by:

$$R_i = W \log(1 + \text{SINR}_i),$$

where $W$ denotes the system bandwidth.

![Block diagram of the MU-beamforming system.](image)
Note that, in this paper, we do not address the calculation of the optimal beamforming weights as done in several studies (e.g. [9] and references therein). We assume that the BS has an arbitrary number of transmit antennas that can provide \( J \) spaced beams per sector as shown in figure 2. The \( J \) pre-defined beams are considered as a fixed codebook either in SU or MU-beamforming modes. This model is used in the subsequent analysis.

### B. Scheduling aspects

We consider a centralized scheduler per radio site which decides at each time slot the set of users to co-schedule on the same time/frequency resource. Different schedulers can be performed as seen in section II-B2 that aim at getting full benefit from multi-user diversity and so improving the system capacity while minimizing the intra-cell interference.

In this work, we consider a Max-Iterate scheduler based on Round Robin which selects a first user at random, blocks all users in the adjacent beams and iterates until reaching the maximum number of active beams or that there are no more users to schedule. The considered MU-scheduling is described in algorithm 1.

At each timeslot

**Input**: Set \( J \) of active beams, \( M \) max number of beams to co-schedule.

**Output**: Set \( U \) of MSs to schedule

**while** \( J \neq 0 \) \& size\( (U) < M \) **do**

- pick at random a MS \( u \), served by beam \( b \in J \);
- \( J \leftarrow J \setminus \{b, b+1[J], b-1[J]\} \);
- \( U \leftarrow U \cup \{u\} \);

**end**

**Algorithm 1**: MU-Scheduling algorithm.

Although this scheduler is simple and does not take into account the radio channel conditions, it remains a good approximation of any opportunistic scheduler like proportional fair when the channel variations are limited or too fast to be exploited.

### C. Traffic aspects

We assume elastic traffic. Data flows arrive according to a Poisson process of intensity \( \lambda \) in the reference cell. Each flow stays in the system as long as the corresponding data have not been successfully transmitted to the MS. Note that the users are assumed to be static during the whole flow duration. Flow sizes are assumed to be independent and exponentially distributed with mean \( \sigma \) bits. The traffic intensity \( \lambda \) in the reference cell is the product \( \lambda \times \sigma \) in bit/s.

### IV. Flow-level Analysis

We start with a SU-beamforming system in the presence of \( J \) serving beams, then we investigate the impact of MU-scheduling under different network configurations.

We focus on a given sector. We consider a set \( C \) of classes of MSs indexed by \( i \) to reflect the different radio conditions in the reference sector. Classes are grouped into subsets \( C_j \) for \( j \in J = \{1, \ldots, J\} \) in the presence of \( J \) serving beams. Since class-\( i \) flows arrive at rate \( \lambda_i \), the corresponding load is:

\[
\rho_i = \frac{\lambda_i \sigma}{R_i},
\]

where \( R_i \) is the transmission rate at class-\( i \) expressed in expression (2).

#### A. SU-beamforming

According to SU-beamforming system, the scheduler selects at random a user covered by a particular beam. This latter is served alone and blocks all other users in the sector. Let \( Z_j(t) \) be the total number of users in beam \( B_j \) at time \( t \), for \( j \in J \). Denote by \( \bar{Z}(t) \) the corresponding vector. Whenever \( \bar{Z}(t) = \bar{z} \), the scheduler selects a user in \( B_j \) a fraction of time of [16]:

\[
\phi_j(\bar{z}) = \frac{\bar{z}_j}{\bar{z}},
\]

where \( \bar{z} \) denotes the total number of users in whole sector.

The queuing system is described by the following transition rates of the Markov process \( \bar{Z}(t) \) from state \( \bar{z} \) to state \( \bar{z}' \):

\[
q(\bar{z}, \bar{z}') = \left\{ \begin{array}{ll}
\lambda_j & \text{for } \bar{z}' = \bar{z} + \bar{e}_j, j \in J \\
\phi_j(\bar{z}) R_j / \sigma & \text{for } \bar{z}' = \bar{z} - \bar{e}_j, j \in J
\end{array} \right.
\]

where \( \bar{e}_j \) is the unit vector on component \( j \), for \( j \in J \).

The system corresponds to a multi-class processor sharing queue with total load \( \bar{\rho} = \sum_{j \in J} \bar{\rho}_j \) where

\[
\bar{\rho}_j = \frac{\lambda_j \sigma}{R_j}.
\]

The arrival rate per beam \( \lambda_j \) is given by

\[
\lambda_j = \sum_{i \in C_j} \lambda_i,
\]

and the mean transmission rate

\[
\bar{R}_j = \frac{\sum_{i \in C_j} p_i \bar{\rho}_i}{\sum \bar{\rho}_i},
\]

with

\[
\sum_{i \in C} p_i = \sum_{i \in C} \lambda_i / \lambda = 1.
\]
In order to investigate the performance of such system, we propose lemma (1).

Lemma 1. Considering a Whittle network [17] of \( J \) queues of load \( \rho_j \), the stationary distribution of the process \( z(t) \) is:

\[
\pi(z) = \pi(0) \Phi(z) \prod_{j=1}^{J} \rho_j^{z_j},
\]

where \( \Phi(z) \) denotes the inverse of the product of service capacities along any direct path from state \( z \) to state 0. Let

\[
G(\rho) = \sum_{z} \Phi(z) \prod_{j=1}^{J} \rho_j^{z_j}.
\]

For each queue \( j \), we have:

- the mean number of users in each queue \( \bar{E}(z_j) \)
  \[
  \bar{E}(z_j) = \rho_j \frac{\partial G(\rho)}{\partial \rho_j} \frac{1}{G(\rho)}.
  \]
- the flow-throughput
  \[
  \gamma_j = R_j \frac{1}{\partial G(\rho_j)} \ln(G(\rho)).
  \]

Proof: Based on the normalization condition where \( \sum_z \pi(z) = 1 \), we have:

\[
\pi(0) = \frac{1}{G(\rho)},
\]

Then, the mean number of users in each queue is given by:

\[
\bar{E}(z_j) = \sum_{z_j \geq 0} z_j \pi(0) \Phi(z) \prod_{j=1}^{J} \rho_j^{z_j}
= \rho_j \frac{\partial G(\rho)}{\partial \rho_j} \frac{1}{G(\rho)}.
\]

The mean sojourn time in each queue follows from Little’s law [18]:

\[
\tau_j = \frac{\bar{E}(z_j)}{\lambda_j}.
\]

Hence, we obtain the flow throughput:

\[
\gamma_j = \frac{\sigma_j}{\tau_j} = R_j \frac{\rho_j}{\bar{E}(z_j)} = R_j \frac{\partial G(\rho)}{\partial \rho_j} \ln(G(\rho)).
\]

We deduce the flow throughput in beam \( B_j \)

\[
\gamma_j = \bar{R}_j (1 - \rho),
\]

The mean throughput in the cell is given by:

\[
\gamma = R(1 - \rho),
\]

where \( R \) refers to the total cell capacity defined as the maximum traffic intensity that can be handled.

We note that the flow throughput decreases linearly with the load from the maximum data rate \( \bar{R}_j \) when \( \rho = 0 \) to \( \gamma = R(1 - \rho) \), although in real cases, this is not a linear decrease since the transmission rates are not fixed and depend on the load of neighboring cells and the caused interference.

B. MU-beamforming

To gain insight into the MU gain, we consider the two-layer beamforming system in the presence of \( J = 3 \) and \( J = 4 \) serving beams per sector.

1) MU-beamforming in the presence of 3 beams: According to the MU-scheduling algorithm aforementioned, the system switches between a SU and MU-beamforming system depending on the first selected user. In fact, if a user covered by the beam \( B_1 \) is selected first, then only those covered by \( B_3 \) are eligible to be selected next. However, when a user in beam \( B_2 \) is selected first, all others covered by adjacent beams namely \( B_1 \) and \( B_3 \) are blocked.

Hence, users in beams \( B_1 \) and \( B_3 \) are a fraction of time of:

\[
\phi_1(\vec{z}) = \phi_3(\vec{z}) = \frac{z_1 + z_3}{z},
\]

and those in beam \( B_2 \) a fraction of time:

\[
\phi_2(\vec{z}) = \frac{z_2}{z}.
\]

The system corresponds to a set of three coupled processor-sharing queues with state-dependent service rates. The queuing system is described by the transition rates given in (3) with \( J = 3 \). This Markov process is reversible and equivalently, the queuing system corresponds to a Whittle network. The stationary distribution of the Markov process \( \vec{Z}(t) \) is then given by:

\[
\pi(\vec{z}) = \frac{(1 - \bar{\rho}_1 - \bar{\rho}_2)(1 - \bar{\rho}_3 - \bar{\rho}_2)}{(1 - \bar{\rho}_2)} \times \left( \frac{\vec{z}}{z_1 + z_3 \bar{\rho}_1 \bar{\rho}_2 \bar{\rho}_3} \right),
\]

under the stability condition that:

\[
\bar{\rho}_1 + \bar{\rho}_2 < 1, \quad \bar{\rho}_3 + \bar{\rho}_2 < 1.
\]

We use lemma (1), we deduce from equation (5) the mean number of flows in each beam

\[
E(z_1) = \frac{\bar{\rho}_1}{1 - \bar{\rho}_1 - \bar{\rho}_2},
\]

\[
E(z_2) = \frac{\bar{\rho}_2}{1 - \bar{\rho}_2} \left( 1 + \frac{\bar{\rho}_1}{1 - \bar{\rho}_1 - \bar{\rho}_2} + \frac{\bar{\rho}_3}{1 - \bar{\rho}_3 - \bar{\rho}_2} \right).
\]
beams
beam
possibility to select another user from another beam (except active or the one at the middle.
the first selected user, either the two beams at extremities are
3 beams switches between SU and MU. In fact, depending on
one half when using MU-beamforming since the system with
scheduling behaviors:
Fig. 3. Normalized user throughput with MU-beamforming with 3 beams.
(a) per beam
(b) in average
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\[ E(z_3) = \frac{\bar{\rho}_3}{1 - \bar{\rho}_3 - \bar{\rho}_2}, \]

and from equation (6) the flow throughput in each beam:

\[ \gamma_1 = \bar{R}_1(1 - \bar{\rho}_1 - \bar{\rho}_2), \quad \gamma_3 = \bar{R}_3(1 - \bar{\rho}_3 - \bar{\rho}_2), \]
\[ \gamma_2 = \frac{\bar{R}_2(1 - \bar{\rho}_2)}{1 + \bar{\rho}_1 - \bar{\rho}_2 + \bar{\rho}_3 - \bar{\rho}_2}. \]

Figure 3 show the results in terms of normalized throughput per beam and in average compared to that obtained with SU-beamforming. We see that the capacity region is improved by one half when using MU-beamforming since the system with 3 beams switches between SU and MU. In fact, depending on the first selected user, either the two beams at extremities are active or the one at the middle.

2) MU-beamforming in the presence of 4 beams: In this case of \( J = 4 \) beams per sector, the scheduling algorithm is always able to select two users from two different beams. In fact, selecting a user from any beam leaves always the possibility to select another user from another beam (except from the adjacent ones). For instance, if a user covered by beam \( B_2 \) is selected, this blocks those covered by adjacent beams \( B_1 \) and \( B_3 \). Then only users covered by beam \( B_2 \) are eligible to be co-scheduled jointly with the selected user from \( B_2 \). However, when a user covered by beam \( B_1 \) is selected, this gives the possibility to users covered by both \( B_3 \) and \( B_4 \) to be scheduled. We differentiate in this case between two scheduling behaviors:

a) Fixed scheduling scheme: As its name suggests, the scheduling scheme in the cell is predefined since the scheduler can either select a user covered by a beam whose index is even or odd. Indeed, if a user covered by \( B_2 \) is selected, then only a user from beam \( B_3 \) can be co-scheduled. Accordingly, at a given time slot, either beams \( B_1 + B_3 \) or \( B_2 + B_4 \) can be active at a given time slot, regardless of their corresponding loads. This can be expressed in terms of fractions of time during which the beams are active:

\[ \phi_1(z) = \frac{z_1 + z_3}{z}, \]
\[ \phi_2(z) = \frac{z_2 + z_4}{z}. \]

The system corresponds in this case to a set of four coupled processor-sharing queues. The queuing system is similar to that described in (3) with \( J = 4 \). The reversibility is maintained and we deduce the stationary distribution of the Markov process \( \bar{Z}(t) \):

\[ \pi(z) = \pi(0) \times \left( \frac{z}{z_1 + z_3, z_2 + z_4} \right) \prod_{i=1}^{4} \bar{\rho}_i, \]

under the stability condition:

\[ \bar{\rho}_1 + \bar{\rho}_3 < 1, \quad \bar{\rho}_2 + \bar{\rho}_4 < 1. \]

For simplicity, we suppose that all beams have the same load such as

\[ \bar{\rho}_j = \bar{\rho}, \forall j \in \mathcal{J}. \]

We use lemma (1) and we deduce from equation (7):

\[ \pi(0) = \frac{(1 - 2\bar{\rho})^3}{1 - 2\bar{\rho} + (2\bar{\rho})^2}. \]

Hence, the mean number of users in each beam \( B_j, \forall j \in \mathcal{J} \), follows from equation (5) so that

\[ E(z_j) = \frac{\bar{\rho}}{(1 - 2\bar{\rho})} \frac{1 - \bar{\rho} + \bar{\rho}^2}{1 - 2\bar{\rho} + 2\bar{\rho}^2}, \]

and the corresponding flow throughput:

\[ \bar{\gamma}_j = \bar{R}_j \left( \frac{\bar{\rho}}{(1 - 2\bar{\rho})} \frac{1 - \bar{\rho} + \bar{\rho}^2}{1 - 2\bar{\rho} + 2\bar{\rho}^2} \right). \]

Note here that \( \bar{R}_j \) refers to the transmission rate in \( B_j \) in the presence of another active beam.

b) Flexible scheduling scheme: Under the flexible scheduling, the load in each beam is taken into account. Indeed, if a user in beam \( B_1 \) is selected, this leaves the possibility to users covered by either beam \( B_3 \) or \( B_4 \) to be co-scheduled depending on their loads. The fractions of time during which beams are active is then given by:

\[ \tilde{\phi}_1(z) = \frac{z_1 + z_3}{z} + \frac{z_4}{z} \frac{z_1}{z_1 + z_2}, \]
\[ \tilde{\phi}_2(z) = \frac{z_2 + z_4}{z} \frac{z_2}{z_1 + z_2}, \]
\[ \tilde{\phi}_3(z) = \frac{z_3}{z} + \frac{z_1}{z} \frac{z_3}{z_3 + z_4}. \]
V. Numerical Results

While the numerical results presented in the previous section were based on normalized rates and aimed at illustrating the derived models, we present in this section a numerical analysis where the analytical models take as input realistic rates from an LTE-advanced simulator.

A. Achievable rates

We first present network simulations results that are used to calculate the achievable rates is SU and MU-beamforming in comparison to a classical system without beamforming. System level evaluation is conducted to compare the performance of a classical system without beamforming to SU-beamforming and MU-beamforming systems in LTE-advanced network settings.

Considering the system parameters summarized in table I, we illustrate in figure 5, the transmission rates at different positions of the reference site on the basis of 100 independent network states. The average values are given in table II in different scenarios. Since our purpose is to evaluate the MU gain of MU-beamforming, we do not consider advanced features of LTE-advanced networks like OFDMA for instance. We assume also that the base station transmit at full power using the whole frequency band.

We see at first that SU-beamforming enables to achieve higher transmission rates compared to a classical system without beamforming. Indeed, concentrating the transmit power on the target MS increases the received power and decreases the interference caused to other MSs. However, with MU-beamforming, the transmission rates are less important due to intra-cell interference caused by the presence of two active beams per cell.

<table>
<thead>
<tr>
<th>TABLE I</th>
<th>SIMULATION PARAMETERS</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parameter</td>
<td>Value</td>
</tr>
<tr>
<td>Site layout</td>
<td>19 sites, 3 sectors per site</td>
</tr>
<tr>
<td>Inter-site distance</td>
<td>500m</td>
</tr>
<tr>
<td>Cell radius</td>
<td>350m</td>
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<tr>
<td>System bandwidth</td>
<td>3MHz</td>
</tr>
<tr>
<td>Carrier frequency band</td>
<td>2.6 GHz</td>
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<tr>
<td>Antenna model</td>
<td>3GPP model [19]</td>
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<tr>
<td>Propagation model</td>
<td>Hata model [20]</td>
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<tr>
<td>Path loss exponent</td>
<td>3.5</td>
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<tr>
<td>Load at neighboring sectors</td>
<td>30%</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>TABLE II</th>
<th>AVERAGE TRANSMISSION RATES</th>
</tr>
</thead>
<tbody>
<tr>
<td>System</td>
<td>Rate (Mbit/s)</td>
</tr>
<tr>
<td>Without beamforming</td>
<td>4.66</td>
</tr>
<tr>
<td>SU-beamforming with 3 beams</td>
<td>7.55</td>
</tr>
<tr>
<td>SU-beamforming with 4 beams</td>
<td>8.02</td>
</tr>
<tr>
<td>MU-beamforming with 3 beams</td>
<td>5.51</td>
</tr>
<tr>
<td>MU-beamforming with 4 beams</td>
<td>4.95</td>
</tr>
</tbody>
</table>
B. Performance results

We address in this section the performance results when combining the Markovian analysis of section (IV) with the network simulations. For different traffic intensities, we plot the average throughput with MU-beamforming and SU-beamforming in comparison to the classical system without beamforming. Results are shown in figure 6.

We notice an important gain of SU-beamforming over the classical system without beamforming and a further gain of MU-beamforming, especially at high loads. Indeed, the system capacity improves considerably by 30% when performing MU-beamforming with 4 beams under the fixed scheduling scheme and around 20% with 3 beams since this system switches between SU and MU-beamforming.

Note that these results are valid for a constant load in neighboring cells (50%). However, in real cases, the flow throughput does not decrease linearly since the transmission rates depend on the interference caused by neighboring cells.

VI. Conclusion

In this paper, we proposed a flow-level modeling of MU-beamforming in cellular networks. We evaluated its performance by combining Markovian analysis with network simulations. We observed that MU-beamforming enables to improve the performance of a SU-beamforming in terms of capacity, especially at high loads. Results were given in a system providing 3 and 4 beams and a maximum of two users to co-schedule. Notice that all the Markovian analysis and the simulation results provided in this work can be easily extended to a higher number of beams and more users to co-schedule. Although the focus of this paper was on single-cell, the framework could be extended to case of multi-cell MU-MIMO (also known as Coordinated Multipoint (CoMP) in LTE-Advanced system) and by considering opportunistic scheduling schemes. This is left as future work.

References


