

# Work in Progress: Intercarrier Compensation between Providers of Different Layers: Advantages of Transmission Initiator Determination

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**Abstract.** This paper addresses the important issue of providing balanced allocation of the interconnection costs between networks. We analyze how beneficial is the determination of the original initiator of a transmission to the providers of different layers. The introduced model, where intercarrier compensation is based on the differentiated traffic flows, was compared with the existing solution, which performs cost compensation based on the traffic flows. For our analysis we considered both unilateral and bilateral settlement arrangements.

**Key words:** Interconnection arrangement, intercarrier compensation, Internet economics.

## 1 Introduction

The Internet is a system of interconnected networks, which are connected either through a direct link or an intermediate point to exchange traffic. Currently, the Internet provides two basic types of interconnections such as peering and transit, and their variations. Peering is the arrangement of traffic exchange on the free-settlement basis, so that Internet service providers (ISPs) do not pay each other and derive revenues from their own customers. In transit, a customer ISP pays a transit ISP to deliver the traffic between the customers. Emergence of new types of ISPs (with large number of customers and great amount of content) led to appearance of new types of models, such as paid peering and partial transit.

Traditionally, before interconnecting, provider calculates whether the interconnection benefits would outweigh the costs [1]. Simple economic principle suggests sharing the costs between all parties. In the case of telephony, the study [2] argued that both calling and called parties benefit from the call, and consequently, should share the interconnection costs. In the Internet, under symmetry of traffic flows, the termination costs are set to zero, since it is assumed that the termination fees are roughly the same, and a peering arrangement is used. However, because no termination cost is charged, settlement-free model is considered

inefficient in terms of cost compensation [3]. Generally, if providers are asymmetric in terms of size, peering is not appropriate, since providers incur different costs and benefit differently. In such a case, an interconnection arrangement is governed by the financial compensation in a bilaterally or unilaterally negotiated basis. In the bilateral settlement arrangements, the payments are based on the net traffic flow. In the unilateral settlement arrangements, a customer provider pays for sent and received traffic, even though traffic flows in both directions. This causes the existence of imbalance in allocation of the interconnection costs. In particular, smaller providers in high cost areas admit higher subscription fees. There exists a large body of literature that discusses interconnection challenges [1, 4-6]. Various pricing schemes have attempted to provide sustainable conditions for smaller ISPs [7-8]. These models make different trade-offs between the two objectives of interconnection pricing, viz., competition development and profitability. Hence, no single model has a clear advantage over the others. As cited in [9], it was recommended to establish bilateral settlement arrangements and to compensate each provider for the costs that it incurs in carrying traffic generated by the other network. However, it was argued that traffic flows are not a reasonable indicator to share the costs, since it is not clear who originally initiated a transmission and, therefore, who should pay for the costs. In other words, compensation between providers cannot be solely done based on the traffic flows, which provide a poor basis for cost sharing [9]. Recently provided analytical studies in [10-11], investigated the impact of the original initiator of a transmission at the wholesale and retail levels in the case of private peering arrangements. Further, we extended studies by examining the benefits of the customer providers only, which purchased transit services [12]. However, the remaining literature on the economics of interconnection considers the intercarrier compensation based only on the flows of traffic [2, 13-16].

The main objective of this paper is to explore the role of the determination of a transmission initiator on ISPs of different layers. The paper differs from the prior reported studies in that it considers how beneficial is the traffic differentiation to *all providers*, such as transit and customer, and it examines customer ISPs, which *operate in different cost areas*. Our studies involve the earlier introduced model, called Differentiated Traffic-based Interconnection Agreement (DTIA) that distinguishes traffic into two types to determine the transmission initiator in the IP networks and to compensate the costs. In contrast to the existing solutions [17], in which the payments are based on traffic flows (TF), we compensate differently for a particular traffic type. Unlike telephony, where the transmission initiator covers the entire costs, imposing uniform retail pricing, the proposed model distributes the joint costs between all parties and supports the diversity of existing retail pricing schemes in the Internet. Comparative studies were provided for the agreements based on the traffic flows and differentiated traffic flows compensations. We considered both unilateral and bilateral settlement models. The rest of the paper is organized as follows. Section 2 discusses existing financial settlements. Section 3 describes the motivation for traffic differentiation. Section 4 provides analytical studies. Section 5 concludes this paper.

## 2 Financial Settlements

Generally, providers arrange financial settlements in order to determine the distribution of the interconnection costs [17]. Before examining financial settlements within the Internet, we consider the telephone system. As an example, assume a scenario, where Alice makes a call to Bob. Accepting the call, Bob incurs termination costs to its provider that should be covered either directly by billing Bob or indirectly by billing the calling party's carrier. As cited in [3], "existing access charge rules and the majority of existing reciprocal compensation agreements require the calling party's carrier, [...], to compensate the called party's carrier for terminating the call". Thus, the initiator of the call, i.e., Alice pays to a subscribed provider for the entire call since Alice asked to reserve the circuit. In contrast to the telephony example, establishing a connection in the Internet does not require any reservation of a circuit. Usually packets between Alice and Bob are routed independently, sometimes even via different paths. Therefore, as cited in [18], "it is very important to distinguish between the *initiator* and the *sender*, and likewise between the *destination* and the *receiver*". The initiator is the party that initiates a call or a session, and the destination is the party that receives a call. In contrast, the sender (the originator) is the party that sends traffic, and the receiver (the terminator) is the party that receives traffic. In telephony, the initiator is considered to be the originator and is charged based on the transaction unit, namely a "call minute" for using the terminating network. Even though it may be argued that a TCP session can be considered as a call, where the initiator of a session pays for the entire traffic flow, such a model deals with technical issues, considerable costs, and implies uniform retail pricing. Currently, the Internet uses the packet-based accounting model, under which the volume of the exchange traffic in both directions is measured, and adopts a small set of interconnection arrangements. Specifically, in the *service-provider* (unilateral) settlement, namely transit and paid peering business relationships, a customer ISP pays to a transit ISP for sent and received traffic. In the *settlement-free* agreement, namely peering relationships, providers do not pay each other. In some cases ISPs adopt the *negotiated-financial* (bilateral) settlement where the payments are based on the net flow of traffic. For detailed discussion see [17-19].

## 3 Motivation for Traffic Differentiation

The principle that we follow is that both parties derive benefits from the exchange of traffic and, therefore, should share the interconnection costs. Considering a system without externalities [20], the costs should be shared based on the benefits obtained by each party. However, in the real world, it is impossible to measure the benefits of parties and so to share the costs. If content is not equally distributed between providers, traffic imbalance occurs, and hence, costs and revenues are not shared evenly. As cited in [21], traffic flow is dominant towards a customer requested the content and generates 85% of the Internet traffic. This implies that inbound traffic is much more compared to outbound

traffic of content request. In telephony for example, it is acceptable that more than 50% of rural network's revenue could come from the incoming calls. In contrast, in the Internet, customer networks pay for the entire traffic flows. It was recommended to compensate each provider for the costs that it incurs in carrying traffic based on the traffic flows. However, traffic flows are not a good measure for costs sharing, since "it is impossible to determine who originally initiated any given transmission on the Internet" and therefore, provide a poor basis for cost sharing [9]. On the other hand, providers are unwilling to inspect the IP header of a packet, since "the cost of carrying an individual packet is extremely small, and the cost of accounting for each packet may well be greater than the cost of carrying the packet across the providers" [19].

The DTIA model presented in [22] manages inter-provider cost compensation considering the original initiator of a transmission. In order to determine a party that originally initiated a transmission, we differentiated traffic into two types, referred to as *native*, which is originally initiated by the provider's own customers, and *stranger* that is originally initiated by the customers of any other network. Indeed, outgoing traffic of ISP<sub>*i*</sub> that is the same as adjacent provider's incoming traffic may be i) either a part of a transmission initiated by a customer of ISP<sub>*i*</sub>, ii) or a part of a transmission initiated by a customer of any other network. Furthermore, we suggest that providers compensate differently for a particular type of traffic, where stranger traffic is charged at a lower rate than native traffic. More specifically, each provider settled DTIA compensates the cost of carrying traffic according to the differentiated traffic flows. For detailed description of the DTIA model and its traffic management mechanism see [22].

## 4 The Model of Interconnection

In our analysis we follow an assumption done in [13] to capture traffic imbalance and therefore, consider two types of the customers, namely websites (*who host information and content*) and consumers (*who use information and content provided on websites*). Actually, traffic is exchanged between consumers, between websites, from websites to consumers, and from consumers to websites. According to the proposed approach, a node (customer) in a P2P network is considered as a *consumer as well as a website simultaneously*, since it can act as a client and as a server. Thus, traffic generated from websites to consumers and vice versa along with Web, FTP and streaming media traffic captures P2P traffic. Traffic between consumers captures VoIP traffic that tends to be symmetric, and email exchange that is much smaller than traffic generated from websites to consumers. To focus on explicit monetary transfers between providers and traffic asymmetry in its simplest way, we consider traffic exchange i) from consumers to websites, and ii) from websites to consumers. To simplify analytical studies the following assumptions were made throughout the paper:

**Assumption 1.** *Let  $\alpha_i \in (0, 1)$  network  $i$ 's market share for consumers and  $\beta_i \in (0, 1)$  its market share for websites. The market consists of only one transit and two customer ISPs,  $i$  and  $j$ , where  $i \neq j = 1, 2$  and  $\alpha_i + \alpha_j = \alpha$ ,  $\beta_i + \beta_j = \beta$ .*

**Assumption 2.** *Balanced calling pattern, where each consumer requests any website in any network with the same probability is considered<sup>1</sup>. Each consumer originates one unit of traffic per each request of website. The number of consumers and websites in the market is given by  $N$  and  $M$  respectively.*

We examine a scenario, in which  $\text{ISP}_i$  and  $\text{ISP}_j$  exchange traffic through the transit  $\text{ISP}_k$ . The amount of the differentiated traffic originated from  $\text{ISP}_i$  with destination to  $\text{ISP}_j$  and vice versa is given by

$$t_{ik}^{nat} = \alpha_i \beta_j NM \quad t_{jk}^{nat} = \alpha_j \beta_i NM \quad (1)$$

$$t_{ik}^{str} = \alpha_j \beta_i NM x \quad t_{jk}^{str} = \alpha_i \beta_j NM x \quad (2)$$

where  $t_{ik}^{nat}$  ( $t_{jk}^{nat}$ ) denotes the amount of outgoing native traffic (exchanged from consumers to websites) and  $t_{ik}^{str}$  ( $t_{jk}^{str}$ ) is the amount of stranger traffic (exchanged from websites to consumers) with respect to  $\text{ISP}_i$  ( $\text{ISP}_j$ ). The variable  $x$  denotes the average amount of traffic caused by requesting a website. It is known that P2P traffic asymmetry is typically caused by less capacity provisioned in the upstream direction. Thus, upstream/downstream P2P traffic flows can be asymmetric, which implies that  $x$  is different for the customers subscribed to different ISPs. However, this does not affect the results of our studies. The total amount of traffic originated by  $\text{ISP}_i$  and  $\text{ISP}_j$  are  $t_{ik} = t_{ik}^{nat} + t_{ik}^{str}$  and  $t_{jk} = t_{jk}^{nat} + t_{jk}^{str}$ .

#### 4.1 Unilateral Settlement Arrangements

We start by considering a unilateral settlement arrangement, where transit ISP charges the customer providers for every unit of traffic sent and received. Let  $c_i^k$  and  $c_j^k$  are the marginal costs of the connectivity of  $\text{ISP}_i$  and  $\text{ISP}_j$  correspondingly. These providers operate in different cost areas so that  $c_i^k < c_j^k$ , where marginal costs exhibit increasing returns to scale (i.e.,  $\text{ISP}_i > \text{ISP}_j$ ).  $\text{ISP}_k$  charges the customer ISPs  $a_k$  and  $b_k$  for every unit of native and stranger traffic respectively, where  $a_k > b_k$  (ISPs pay less for stranger traffic). In particular, in DTIA we consider that a customer ISP i) compensates fully the imbalance in the connectivity costs between endpoints, if the exchanged traffic is native, and ii) does not compensate this difference, if the originated traffic is stranger. The difference in the costs of the exchanged traffic between the points is defined by

$$\Delta = c_j^k - c_i^k \quad (3)$$

**Proposition 1.** *The access charge for stranger traffic is set to the lowest cost of the connectivity, i.e.,  $b_k = c_i^k$ .*

*Proof.* Interconnection costs between the customer providers are covered by the access charges. Since native traffic for  $\text{ISP}_i$  is stranger for  $\text{ISP}_j$ , the sum of fees for native and stranger traffic are equal to the whole costs, that is

$$c_i^k + c_j^k = a_k + b_k \quad (4)$$

<sup>1</sup> Due to the lack of mathematical models on how traffic between ISPs is distributed, many works make a statistical assumption, such as balanced calling pattern.

In the DTIA model, a provider compensates the imbalance in the costs expressed by (3) fully only for native traffic. This cost difference is not compensated for the stranger traffic. Consequently, it can be written that

$$a_k = b_k + \Delta \quad (5)$$

By substituting (3) and (5) in (4), it can be obtained that access rate for stranger traffic is set to the lowest cost of the connectivity, that is  $b_k = c_i^k$ . Obviously, that the access charge for native traffic is defined by  $a_k = c_i^k + \Delta$ .  $\square$

We investigate the payments of the customer providers in the classical and DTIA models. The payments of ISP<sub>*i*</sub> and ISP<sub>*j*</sub> to transit ISP in DTIA are given by

$$f_{ik} = a_k(t_{ik}^{nat} + t_{jk}^{str}) + b_k(t_{ik}^{str} + t_{jk}^{nat}) \quad (6)$$

$$f_{jk} = a_k(t_{jk}^{nat} + t_{ik}^{str}) + b_k(t_{jk}^{str} + t_{ik}^{nat}) \quad (7)$$

The sum of these payments presents the incremental revenue of the transit ISP  $\pi_k = f_{ik} + f_{jk}$ . The net payments of the customer ISPs according to the traffic flow based compensation are denoted by  $\check{f}_{ik}$  and  $\check{f}_{jk}$  and calculated as follows

$$\check{f}_{ik} = c_i^k(t_{ik} + t_{jk}) \quad (8)$$

$$\check{f}_{jk} = c_j^k(t_{ik} + t_{jk}) \quad (9)$$

**Proposition 2.** *The payments of larger (smaller) providers are higher (less) in DTIA than these in the classical model.*

*Proof.* Considering the net payments of the larger ISP<sub>*i*</sub>, from (6) and (8) follows that  $\check{f}_{ik} - f_{ik} = (b_k - a_k)(t_{ik}^{nat} + t_{jk}^{str}) < 0$ , i.e.,  $f_{ik} > \check{f}_{ik}$ . Similarly, comparing the payments of ISP<sub>*j*</sub> in the DTIA and classical models given by (7) and (9) we obtain that  $\check{f}_{jk} - f_{jk} = (a_k - b_k)(t_{ik}^{nat} + t_{jk}^{str}) > 0$ . This gives that  $f_{jk} < \check{f}_{jk}$ .  $\square$

## 4.2 Bilateral Settlement Arrangements

This subsection examines bilateral settlement models, where each provider (including customer ISP) is compensated for the costs of carrying traffic.

**Reciprocal Access Charges** In the following lines we explore the case when the customer providers charge the transit provider reciprocal access charges and vice versa. Let  $b$  be the access payment that ISP<sub>*k*</sub> subsidizes ISP<sub>*i*</sub> and ISP<sub>*j*</sub> for every unit of sent traffic, where  $b < c_j^k$ . The marginal connectivity costs of the customer providers charged by ISP<sub>*k*</sub> can be written as follows

$$c_i^k + c_j^k = c_k + \sigma \quad (10)$$

where  $c_k$  is the marginal transportation cost of ISP<sub>*k*</sub>;  $\sigma$  is an arbitrary constant.

**Proposition 3.** *The access charge for stranger traffic set by ISP<sub>*k*</sub> is equal to  $b_k = c_k + b$  (i.e., the total costs of ISP<sub>*k*</sub>).*

*Proof.* The costs of  $ISP_k$  are comprised of the marginal transmission cost and the payment to access customer provider's infrastructure, i.e.,  $c_k + b$ . The bilateral settlement model is attractive to  $ISP_k$  only if its own costs are covered. These costs correspond to the minimum level of access charge set by  $ISP_k$ , that is

$$c_k + b = \min\{a_k, b_k\}$$

In DTIA provider compensates less the costs of carrying stranger traffic, thus

$$b_k = c_k + b \quad (11)$$

Obviously, that the access charge for native traffic set by the transit provider is increased by the arbitrary constant and calculated as follows  $a_k = b_k + \sigma$ .  $\square$

The net interconnection payments from  $ISP_i$  and  $ISP_j$  to  $ISP_k$  are defined by

$$f_{ik} = a_k t_{ik}^{nat} + b_k t_{ik}^{str} \quad f_{jk} = a_k t_{jk}^{nat} + b_k t_{jk}^{str} \quad (12)$$

Analogously, the net transfers of  $ISP_k$  to the customer providers are given by

$$f_{ki} = b(t_{jk}^{nat} + t_{jk}^{str}) \quad f_{kj} = b(t_{ik}^{nat} + t_{ik}^{str}) \quad (13)$$

It can be noticed that the transit ISP is charged based on the rate for stranger traffic, because we consider that it does not have any customers of its own.

Before examining the payments of the customer ISPs in the DTIA and classical models with bilateral settlements, we consider access charges and net payments in the classical solution. Let  $\check{b}$  be the payment paid by  $ISP_k$  to the customer providers for sending traffic. In the model with bilateral settlements, the access charge set by the transit provider is defined by  $\check{a}_k = c_i^k + c_j^k + \check{b}$ . Assume that  $ISP_k$  has users, thus  $b$  (in DTIA) is the rate charged by the customer ISPs for unit of stranger traffic only, while  $\check{b}$  (in the classical model) is payment for unit of traffic. As a result, we obtain that  $\check{b} \geq b$ . The payments of  $ISP_i$  and  $ISP_j$  are

$$\check{f}_{ik} = \check{a}_k t_{ik} \quad \check{f}_{jk} = \check{a}_k t_{jk} \quad (14)$$

**Proposition 4.** *The net payments of the customer providers in the DTIA model are less than these in the classical model.*

*Proof.* Considering the payments of  $ISP_i$  and  $ISP_j$  given by (12) and (14) follows

$$\check{f}_{ik} - f_{ik} = t_{ik}^{nat}(\check{a}_k - a_k) + t_{ik}^{str}(\check{a}_k - b_k) > 0 \quad (15)$$

$$\check{f}_{jk} - f_{jk} = t_{jk}^{nat}(\check{a}_k - a_k) + t_{jk}^{str}(\check{a}_k - b_k) > 0 \quad (16)$$

$\square$

**Non-reciprocal Access Charges** We continue with examination of the bilateral settlement model with asymmetric access fees. Let  $b_i$  and  $b_j$  ( $b_i < b_j$ ) are the access rates for every unit of traffic received by  $ISP_i$  and  $ISP_j$  correspondingly.

Following the results of Proposition 3, fees that the transit provider charges the customer ISPs for native and stranger traffic can be rewritten as

$$\begin{aligned} a_{ik} &= c_i^k + c_j^k + b_j & a_{jk} &= c_i^k + c_j^k + b_i \\ b_{ik} &= c_k + b_j & b_{jk} &= c_k + b_i \end{aligned}$$

The net payments from ISP<sub>*i*</sub> and ISP<sub>*j*</sub> to the transit ISP<sub>*k*</sub> and vice versa are

$$f_{ik} = a_{ik}t_{ik}^{nat} + b_{ik}t_{ik}^{str} \quad f_{jk} = a_{jk}t_{jk}^{nat} + b_{jk}t_{jk}^{str} \quad (17)$$

$$f_{ki} = b_i \left( t_{jk}^{nat} + t_{jk}^{str} \right) \quad f_{kj} = b_j \left( t_{ik}^{nat} + t_{ik}^{str} \right) \quad (18)$$

The following lines explore the payments of customer ISPs in the classical and DTIA models. For this purpose, we consider access charges and payments in the classical solution. The access rates that ISP<sub>*k*</sub> charges ISP<sub>*i*</sub> and ISP<sub>*j*</sub> are

$$\check{a}_{ik} = c_i^k + c_j^k + \check{b}_j \quad \check{a}_{jk} = c_i^k + c_j^k + \check{b}_i$$

where  $\check{b}_i$  and  $\check{b}_j$  ( $\check{b}_i \geq b_i$ ,  $\check{b}_j \geq b_j$ ) are access fees set by the customer providers correspondingly. The net payments of the customer providers are given by

$$\check{f}_{ik} = \check{a}_{ik}t_{ik} \quad \check{f}_{jk} = \check{a}_{jk}t_{jk} \quad (19)$$

**Proposition 5.** *The interconnection payments of the customer providers are less in DTIA than these in the classical model.*

*Proof.* Examining the payments of ISP<sub>*i*</sub> and ISP<sub>*j*</sub> given by (17) and (19) follows

$$\check{f}_{ik} - f_{ik} = t_{ik}^{nat}(\check{a}_{ik} - a_{ik}) + t_{ik}^{str}(\check{a}_{ik} - b_{ik}) > 0 \quad (20)$$

$$\check{f}_{jk} - f_{jk} = t_{jk}^{nat}(\check{a}_{jk} - a_{jk}) + t_{jk}^{str}(\check{a}_{jk} - b_{jk}) > 0 \quad (21)$$

□

### 4.3 Discussions

Tables 1-3 report the results of analytical studies, which examined how beneficial is the determination of a transmission initiator to the providers of different layers. The comparison results between unilateral settlement models are presented in Table 1. Tables 2 and 3 demonstrate the comparison of bilateral settlement arrangements with symmetric and asymmetric access charges. The analyses considered all available market states in terms of providers' market shares, where  $\text{ISP}_i > \text{ISP}_j$ . The following parameter values were imposed to calculate the specific outcomes:  $c_i^k = 0.4$ ,  $c_j^k = 1.5$ ,  $c_k = 0.9$ ,  $b = 0.5$ ,  $b_i = 0.3$ ,  $b_j = 0.5$ ,  $x = 35$ ,  $N = 100$ , and  $M = 60$ . In order to simplify analyses we assume that  $\check{b} = b$ ,  $\check{b}_i = b_i$ , and  $\check{b}_j = b_j$ . The parameters are chosen to satisfy a condition that providers operate in different cost areas. However, the specification is clearly arbitrary. It is important to note, that our conclusions do not heavily depend on



the chosen parameter values. The results obtained for a number of other parameter sets have not produced significant changes. Network  $i$ 's total incremental cost of connectivity is defined by  $r_i = f_{ik} - f_{ki}$ . Network  $k$ 's profit obtained from interconnection is  $r_k = (f_{ik} + f_{jk}) - (f_{ki} + f_{kj})$ .

Comparative results obtained for arrangements with unilateral settlements demonstrated that in the presented model the payments are decreased for the smaller ISP and are increased for the larger ISP. This is achieved by different access rates charged for the distinguished traffic flows. Specifically, the payments of ISP $_i$  are increased due to native traffic compensation, while the payments of ISP $_j$  are decreased due to stranger traffic compensation. Further, the results showed that in DTIA the more outgoing traffic the lower costs of the provider. In particular, incoming and outgoing native traffic are directly proportional. Hence, the network that sends more native traffic incurs higher costs than the network that receives this traffic. This is explained by the higher access charges for native than stranger traffic. The costs of both customer ISPs are equal only in the case when their native and stranger traffic volumes are symmetric correspondingly. Finally, the results indicated that the revenues of the transit provider in the classical model based on the traffic flows compensation and DTIA are equal.

The key consequences provided below are based on the analytical studies, which explored bilateral settlement arrangements. In DTIA, the payments paid by the customer providers are decreased and these of transit provider remain the same. Specifically, providers ISP $_i$  and ISP $_j$  compensate based on the differentiated traffic flows, where the access charge for stranger traffic flow is lower than the access charge set in the classical model. As a consequence, the total incremental costs of the customer providers ( $r_i$  and  $r_j$ ) are also decreased. On the other side, profits of ISP $_k$  obtained from the interconnection (i.e., the differences between received and paid payments,  $r_k$ ) are lower than these in the traffic flow based compensation model. However, as mentioned earlier, it was argued that traffic flows provide a poor basis for Internet interconnection cost sharing.

The provided studies examined a model consisting of one transit and two customer ISPs. One question that arises here is on the robustness of the obtained results for more realistic scenarios, which consider more transit and customer ISPs. From Propositions 2, 4 and 5 it can be noticed that the results depend only on the access charges of both DTIA and classical models. More specifically, in the unilateral settlement arrangements, the results rely on the inequality  $(a_k - b_k) > 0$ . Analogously, the results given by (15) and (16) depend on the inequalities  $(\check{a}_k - a_k) > 0$  and  $(\check{a}_k - b_k) > 0$ , while results expressed by (20) and (21) are based on  $(\check{a}_{ik} - a_{ik}) > 0$  and  $(\check{a}_{ik} - b_{ik}) > 0$ . Hence, the provided conclusions remain the same. Obviously, in the extended scenarios, access charges are obtained by solving a system of linear equations.

## 5 Summary and Conclusions

In this paper we proposed models and their analysis, which are based on the DTIA strategy for inter-provider cost compensation. The goal for this was to ex-

**Table 1.** Comparative Results of DTIA with Unilateral Settlements.

Case	$\alpha_i$	$\beta_i$	$t_{ik}^{nat}$	$t_{jk}^{nat}$	$t_{ik}$	$t_{jk}$	$f_{ik}$		$f_{jk}$		$\pi_k$	
							DTIA	TF	DTIA	TF	DTIA	TF
<b>I</b>	0.5	0.9	300	2700	94800	13200	55080	43200	150120	162000	205200	205200
$\alpha_i = \alpha_j$	0.5	0.8	600	2400	84600	23400	66960	43200	138240	162000	205200	205200
$\beta_i > \beta_j$	0.5	0.7	900	2100	74400	33600	78840	43200	126360	162000	205200	205200
<b>II</b>	0.9	0.5	2700	300	13200	94800	150120	43200	55080	162000	205200	205200
$\alpha_i > \alpha_j$	0.8	0.5	2400	600	23400	84600	138240	43200	66960	162000	205200	205200
$\beta_i = \beta_j$	0.7	0.5	2100	900	33600	74400	126360	43200	78840	162000	205200	205200
<b>III</b>	0.9	0.8	1080	480	17880	38280	65232	22464	41472	84240	106704	106704
$\alpha_i > \alpha_j$	0.8	0.7	1440	840	30840	51240	89856	32832	66096	123120	155952	155952
$\beta_i > \beta_j$	0.7	0.6	1680	1080	39480	59880	106272	39744	82512	149040	188784	188784
$\alpha_i > \beta_i$	0.6	0.55	1620	1320	47820	58020	106488	42336	94608	158760	201096	201096
<b>IV</b>	0.9	0.9	540	540	19440	19440	36936	15552	36936	58320	73872	73872
$\alpha_i > \alpha_j$	0.8	0.8	960	960	34560	34560	65664	27648	65664	103680	131328	131328
$\beta_i > \beta_j$	0.7	0.7	1260	1260	45360	45360	86184	36288	86184	136080	172368	172368
$\alpha_i = \beta_i$	0.6	0.6	1440	1440	51840	51840	98496	41472	98496	155520	196992	196992
<b>V</b>	0.9	0.2	4320	120	8520	151320	235008	63936	68688	239760	303696	303696
$\alpha_i > \alpha_j$	0.8	0.25	3600	300	14100	126300	198720	56160	68040	210600	266760	266760
$\beta_i < \beta_j$	0.7	0.35	2730	630	24780	96180	156492	48384	73332	181440	229824	229824

**Table 2.** Comparative Results of Bilateral Settlement Arrangements (Reciprocal Access Charges).

Case	$f_{ik}$		$f_{jk}$		$f_{ki}$	$f_{kj}$	$r_k$		$r_i$		$r_j$	
	DTIA	TF	DTIA	TF			DTIA	TF	DTIA	TF	DTIA	TF
<b>I</b>	133020	227520	21180	31680	6600	47400	100200	205200	126420	220920	-26220	-15720
	119040	203040	35160	56160	11700	42300	100200	205200	107340	191340	-7140	13860
	105060	178560	49140	80640	16800	37200	100200	205200	88260	161760	11940	43440
<b>II</b>	21180	31680	133020	227520	47400	6600	100200	205200	-26220	-15720	126420	220920
	35160	56160	119040	203040	42300	11700	100200	205200	-7140	13860	107340	191340
	49140	80640	105060	178560	37200	16800	100200	205200	11940	43440	88260	161760
<b>III</b>	26112	42912	54072	91872	19140	8940	52104	106704	6972	23772	45132	82932
	44616	74016	72576	122976	25620	15420	76152	155952	18996	48396	57156	107556
	56952	94752	84912	143712	29940	19740	92184	188784	27012	64812	65172	123972
	68568	114768	82548	139248	29010	23910	98196	201096	39558	85758	58638	115338
<b>IV</b>	27756	46656	27756	46656	9720	9720	36072	73872	18036	36936	18036	36936
	49344	82944	49344	82944	17280	17280	64128	131328	32064	65664	32064	65664
	64764	108864	64764	108864	22680	22680	84168	172368	42084	86184	42084	86184
	74016	124416	74016	124416	25920	25920	96192	196992	48096	98496	48096	98496
<b>V</b>	16248	20448	211968	363168	75660	4260	148296	303696	-59412	-55212	207708	358908
	23340	33840	177120	303120	63150	7050	130260	266760	-39810	-29310	170070	296070
	37422	59472	135282	230832	48090	12390	112224	229824	-10668	11382	122892	218442

**Table 3.** Comparative Results of Bilateral Settlement Models (Non-reciprocal Access Charges).

Case	$f_{ik}$		$f_{jk}$		$f_{ki}$	$f_{kj}$	$r_k$		$r_i$		$r_j$	
	DTIA	TF	DTIA	TF			DTIA	TF	DTIA	TF	DTIA	TF
I	133020	227520	18540	29040	3960	47400	100200	205200	129060	223560	-28860	-18360
	119040	203040	30480	51480	7020	42300	100200	205200	112020	196020	-11820	9180
	105060	178560	42420	73920	10080	37200	100200	205200	94980	168480	5220	36720
II	21180	31680	114060	208560	28440	6600	100200	205200	-7260	3240	107460	201960
	35160	56160	102120	186120	25380	11700	100200	205200	9780	30780	90420	174420
	49140	80640	90180	163680	22320	16800	100200	205200	26820	58320	73380	146880
III	26112	42912	46416	84216	11484	8940	52104	106704	14628	31428	37476	75276
	44616	74016	62328	112728	15372	15420	76152	155952	29244	58644	46908	97308
	56952	94752	72936	131736	17964	19740	92184	188784	38988	76788	53196	111996
	68568	114768	70944	127644	17406	23910	98196	201096	51162	97362	47034	103734
IV	27756	46656	23868	42768	5832	9720	36072	73872	21924	40824	14148	33048
	49344	82944	42432	76032	10368	17280	64128	131328	38976	72576	25152	58752
	64764	108864	55692	99792	13608	22680	84168	172368	51156	95256	33012	77112
	74016	124416	63648	114048	15552	25920	96192	196992	58464	108864	37728	88128
V	16248	20448	181704	332904	45396	4260	148296	303696	-29148	-24948	177444	328644
	23340	33840	151860	277860	37890	7050	130260	266760	-14550	-4050	144810	270810
	37422	59472	116046	211596	28854	12390	112224	229824	8568	30618	103656	199206

plore how the determination of a transmission initiator affects different providers, operated in different cost areas and arranged interconnection with unilateral and bilateral settlements (Tables 1-3). The results obtained from the analytical studies showed that DTIA was able to find better results (in terms of interconnection payments) than the classical solution for the both models. More specifically, the proposed scheme diminishes the existing inequity in allocation of the interconnection costs. From the comparison between unilateral settlement models follows that the costs of the smaller provider are decreased. This stimulates the retail prices fall in the market, where the provider operates and consequently, the development of the infrastructure in terms of subscribed customers. The growth of the smaller ISP leads to balance the volumes of a particular traffic type, and as a result, reduces the imbalance in cost allocation. Obviously, that revenue of the larger ISP obtained from retail market will be increased. From the perspective of a transit provider, its revenues obtained from the customer providers remain the same in the DTIA and classical models.

In the bilateral settlement arrangements, the net payments of both customer ISPs in the DTIA model are decreased. This leads to the decrease in the incremental revenue obtained by the transit provider. Finally, the comparison between the existing model with unilateral settlement and DTIA with bilateral settlement showed that our approach generally performed better for both smaller and larger ISPs in terms of reduced net payments. For the smaller provider, DTIA is

dominated in all cases over the classical model, and for the larger provider only in Cases II and V. Obviously, that the profits of the transit provider in bilateral settlement model are decreased, since it along with other ISPs shares the interconnection costs. Resuming, the provision of a model, which compensates providers while exploiting their infrastructures, is advantageous for sustainable environment. From this point of view the proposed DTIA model is beneficial.

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