

# Extended Dominating Set in Ad Hoc Networks Using Cooperative Communication <sup>\*</sup>

Jie Wu, Mihaela Cardei, Fei Dai, and Shuhui Yang

Department of Computer Science and Engineering  
Florida Atlantic University  
Boca Raton, FL 33431

**Abstract.** We propose a notion of extended dominating set whereby each node in an ad hoc network is covered by either a dominating neighbor or several 2-hop dominating neighbors. This work is motivated by cooperative communication in ad hoc networks where transmitting independent copies of a packet generates diversity and combats the effects of fading. In this paper we propose several efficient heuristic algorithms for constructing a small extended dominating set.

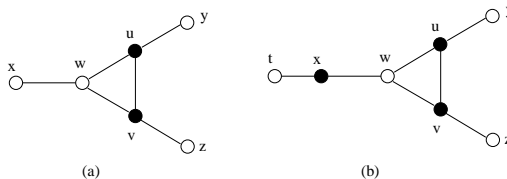
## 1 Introduction

Dominating set (DS) has been widely used in ad hoc networks. A set is dominating if every node in the network is either in the set or a neighbor of a node in the set. When a DS is connected (i.e., its induced graph is connected), it is denoted as CDS. The problem of finding the minimum DS and minimum CDS is NP-complete. Many heuristic protocols have been proposed to find a minimal DS or CDS [1] [2] [3].

We propose a notion of *extended dominating set* based on *cooperative communication* (CC) [4]. CC makes single-antenna nodes in a multi-user scenario share their antennas to create a virtual multiple-input multiple-output (MIMO) system. CC can potentially combine the following two advantages: (1) the power savings provided by multi-hopping, and (2) the spatial diversity provided by the antennas of separate mobile nodes. In CC, transmitting independent copies of a packet generates diversity and combats the effects of fading. In this way,  $k$  copies of the same packet can potentially reach a receiver outside the normal transmission range without increasing transmit power. Under the CC model, a DS is called an extended dominating set (EDS) if, for every node in the network, it is in the set, it has a neighbor in the set, or it has  $k$  2-hop neighbors in the set. In Fig. 1 (a),  $\{u, v, w\}$  forms a CDS. If using CC, and  $k = 2$ , node  $x$  is covered by two 2-hop neighbors,  $u$  and  $v$ . Then,  $w$  can be withdrawn and  $\{u, v\}$  forms an EDS. Since the set is connected, it is also called an *extended connected dominating set* (ECDS). Later, we will define weakly connected EDS (EWCDS). In EWCDS, the broadcast will be successful for at least one source in EDS; whereas in the ECDS the broadcast will be successful for any source in the EDS. In Fig. 1 (b),  $\{u, v, x\}$  forms an EWCDS for  $k = 2$  since  $x$  can retrieve the complete packet when either  $u$  or  $v$  is the source, while neither  $u$  nor  $v$  can when  $x$  is the source.

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**Fig. 1.** (a) A sample with CDS:  $\{u, v, w\}$  and ECDS:  $\{u, v\}$ . (b) EWCDS:  $\{x, u, v\}$ .

Wu and Lou [5] classified CDS formation methods into *global*, *quasi-global*, *quasi-local*, and *local* depending on the amount of information each node has, and the complexity of both message and time to determine a CDS. This paper focuses on some non-trivial extensions of various methods for ECDS/EWCDS and proposes (1) global solutions for EWCDS, (2) quasi-global solutions for EWCDS, (3) quasi-local solutions for EDS and ECDS, and (4) local solutions for EDS and ECDS. For more technical details, theorem proofs and simulation results, readers are referred to [6].

## 2 Extended Dominating Set

Given a set  $V$  of points in a 2D space, a normal transmission range  $r$ , and a CC range  $r'$ , we define a graph with vertex set  $V$  and an arc from vertex  $v$  to vertex  $u$  iff the Euclidean distance,  $d(v, u)$ , is no more than  $r$ . In addition, we define a quasi-arc from vertex  $v$  to vertex  $u$  iff  $r < d(v, u) \leq r'$ . When  $r' = 2r$ , the corresponding graph can be approximated by a single unit disk graph, where a quasi-arc exists between any two vertices (called quasi neighbors) that are separated by two hops.

**Definition 1.** A subset of nodes is an EDS if every node is (a) in the subset, (b) a regular neighbor of a node in the subset, or (c) a quasi neighbor of  $k$  nodes in the subset.

**Definition 2.** An EDS is strongly connected under the CC model (denoted as ECDS) if for any node  $u$  in the set sending a packet, the packet should be fully received by all other nodes eventually. Only nodes with a fully received packet (including  $u$ ) are able to forward the packet once.

If the connectivity condition holds for at least a particular node  $u$ , it is called *weakly connected* (EWCDS). It is known that DS and CDS problems in unit disk graphs are NP-complete. We proved that EDS, ECDS, and EWCDS problems are NP-complete.

The ECDS/EWCDS can be used as a virtual backbone under the CC model. Such a backbone can support an efficient broadcast process and reduce searching space. Unlike broadcasting using regular DS, the source node may need a relay node (not in the EDS) to forward the packet to a node in the EDS; otherwise, only the nodes in the EDS need to forward the packet.

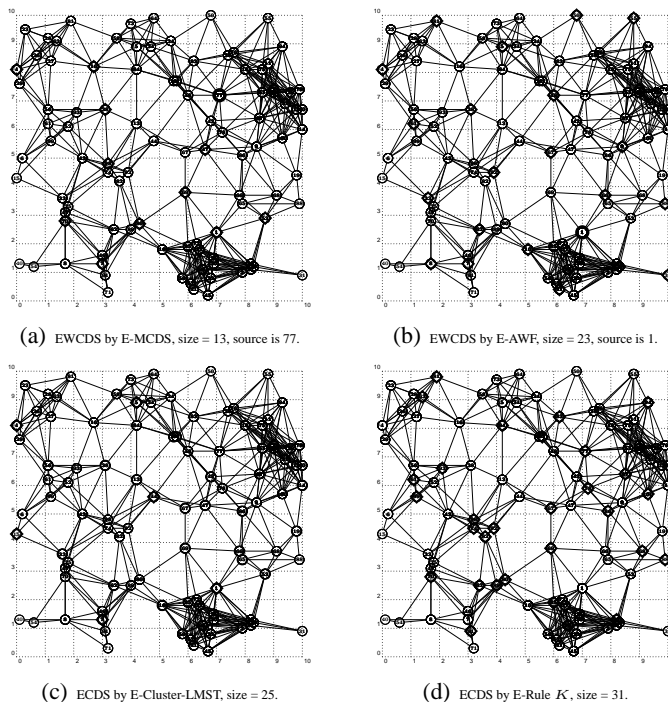


Fig. 2. Sample ECDS or EWCDs in an ad hoc network with 100 nodes.

### 3 Heuristic Solutions

**Global solutions for EWCDs.** We consider a centralized greedy solution called extended MCDS (E-MCDS), based on Guha and Khuller’s MCDS [1]. MCDS “grows” a tree from a selected root until all nodes are covered. Non-leaf nodes form a CDS. We introduce the notion of *contribution* here: Each forward node contributes 1 to all its neighbors and  $1/k$  to all quasi neighbors. The *reception ratio* of a node is the combined contribution of its forward (quasi) neighbors. The algorithm is to find a minimum EWCDs so that all other nodes are *reachable* (i.e., each node has a reception ratio of at least 1). To ensure a constant approximation ratio, we employ a *mutual exclusion rule* which uses the concept of independent set. Fig. 2 (a) shows the EWCDs generated by the E-MCDS in a random, 100-node connected graph.

**Quasi-global solutions for EWCDs.** We extend the AWF algorithm [2] for CDS. AWF contains topology sorting, sequential clustering, and gateway designation procedures. In our extended AWF algorithm for EWCDs (E-AWF), we modify the gateway designation procedure to use an extended gateway designation approach, thus the set of selected nodes becomes an EWCDs, and the algorithm has a constant approximation ratio. Fig. 2 (b) shows the EWCDs generated by E-AWF.

**Quasi-local solutions for EDS and ECDS.** We use the clustering approach as the solution for EDS and ECDS. By a quasi-local solution, we mean the solution completes with a high probability in a small number of rounds with an occasional large number of rounds for completion. The clustering algorithm contains the selection of clusterheads and gateways. In our extended clustering approach (E-Clustering), each node operates on its 2-hop neighborhood. When a clusterhead is chosen, it does not only contribute 1 to the coverage of its neighbors, but also  $1/k$  to its quasi neighbors. To extend EDS to ECDS, we use an extension of the local minimum spanning tree (LMST) algorithm [7] to select gateways, whereby the 1-hop neighborhood includes the current clusterhead, all clusterheads within 5 hops, and their pairwise minimum “virtual path” in terms of hop count. In this way, each pair of neighboring clusterheads has a virtual link and LMST can be applied. The EDS generated by extended clustering and gateway nodes together forms an ECDS that has a constant approximation ratio. In Fig. 2 (c), the clusterheads are noted by diamonds, and the gateways by bold circles.

**Local Solutions for EDS and ECDS.** In local backbone construction, each node maintains only 2-hop information and performs: (1) Dai and Wu’s pruning rule [3] (Rule  $K$ ) for constructing a CDS, and (2) an aggressive pruning rule to remove nodes from the CDS while still maintaining local coverage and connectivity. We develop the extended Rule  $K$  (E-Rule  $K$ ), which uses 2-hop information, including the markers of all 2-hop neighbors. A marked node  $u$  can be unmarked if all its 2-hop neighbors, regular and quasi, can be covered (including contribution cumulation) by other marked nodes with higher priority (noted as  $C$ ) in the neighborhood, and the corresponding condition is called the *coverage condition*. The set derived by the pruning rule based on the coverage condition forms an EDS. To ensure connectivity, we require  $C$  to be connected under the CC model, the *connectivity condition*. We call  $C$  an *extended component* if it is strongly connected (based on Definition 2). A pruning rule that meets coverage and connectivity conditions preserves an ECDS with the expected size  $O(1) \cdot |ECDS_{opt}|$ , where  $ECDS_{opt}$  is an optimal solution to the ECDS problem. Fig. 2 (d) shows the ECDS generated by the E-Rule  $K$ .

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